

# Calculus Web Assignments

Web Assignments are intended to be completed with a partner. Both partners should individually work each of the problems, followed by a collaborative discussion about the problem.

Both partners are required to participate in the “Honor-System” Grading of the Web Assignment.

## Calculus: Web Assignment #22

### Multiple Choice

Identify the choice that best completes the statement or answers the question.

\_\_\_\_\_ 1. Find the indefinite integral  $\int 2 \sec y (\tan y - \sec y) dy$ .

- a.  $2 \sec y \tan y + C$
- b.  $2 \sec y - 2 \tan y + C$
- c.  $2 \sec y + \tan y + C$
- d.  $2 + 2 \sec y + C$
- e.  $2 \sec y \tan y - 2 \sec y + C$

\_\_\_\_\_ 2. Solve the differential equation.

$$\frac{dP}{dx} = 15x^4 - 5, \quad P(-2) = 8$$

- a.  $P(x) = 3x^5 + 5x$
- b.  $P(x) = 3x^5 + 94$
- c.  $P(x) = 3x^5 - 5x + 94$
- d.  $P(x) = 60x^3 - 5x + 94$
- e.  $P(x) = 3x^5 + C$

\_\_\_\_\_ 3. Use left endpoints and 10 rectangles to find the approximation of the area of the region between the graph of the function  $4x^2 - x - 1$  and the  $x$ -axis over the interval  $[4, 14]$ . Round your answer to the nearest integer.

- a. 2925
- b. 3325
- c. 3000
- d. 3250
- e. 3125

\_\_\_\_\_ 4. Write the limit  $\lim_{|\Delta x| \rightarrow 0} \sum_{i=1}^n 4c_i(7 - c_i)^2 \Delta x_i$ , as a definite integral on the interval  $[0, 8]$  where  $c_i$  is any point in the  $i^{\text{th}}$  subinterval.

a.  $\int 4x(7 - x)^8 dx$

b.  $\int_0^8 4x^2(7 - x)^8 dx$

c.  $\int 4c_i(7 - c_i)^2 \Delta x_i$

d.  $\int_0^8 4x(7 - x)^2 dx$

e.  $\int_0^{c_i} 4c_i(7 - c_i)^2 \Delta x_i$

\_\_\_\_\_ 5.  $\frac{d}{dx} \int_2^x \sqrt{1+t^2} dt =$

a.  $\frac{x}{\sqrt{1+x^2}}$

b.  $\sqrt{1+x^2} - 5$

c.  $\sqrt{1+x^2}$

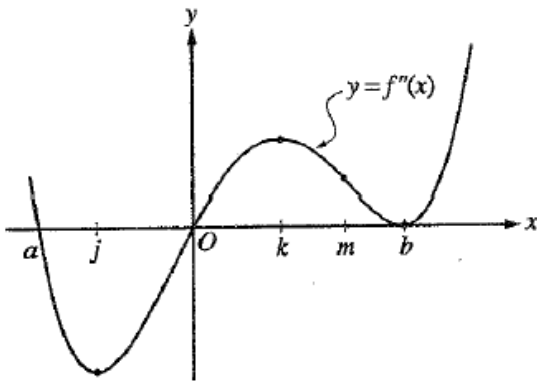
d.  $\frac{x}{\sqrt{1+x^2}} - \frac{1}{\sqrt{5}}$

e.  $\frac{1}{2\sqrt{1+x^2}} - \frac{1}{2\sqrt{5}}$

\_\_\_\_\_ 6. What are the values of  $x$  for which the function  $f$  defined by  $f(x) = (x^2 - 3)e^{-x}$  is decreasing?

- a. There are no such value of  $x$ .
- b.  $x < -1$  and  $x > 3$
- c.  $-3 < x < 1$
- d.  $-1 < x < 3$
- e. All values of  $x$

7.



The second derivative of the function  $f$  is given by

$f''(x) = x(x - a)(x - b)^2$ . The graph of  $f''$  is shown above.

For what values of  $x$  does the graph of  $f$  have a point of inflection?

- a. 0 and  $a$  only
- b. 0 and  $m$  only
- c.  $b$  and  $j$  only
- d. 0,  $a$ , and  $b$
- e.  $b$ ,  $j$ , and  $k$

8. The  $\lim_{x \rightarrow 0} \frac{\tan 3(x + h) - \tan 3x}{h}$  is

- a. 0
- b.  $3 \sec^2(3x)$
- c.  $\sec^2(3x)$
- d.  $3 \cos(3x)$
- e. nonexistent

\_\_\_\_\_ 9. Let R represent the region enclosed by the graphs  $y = x$  and  $y = x^2$  over the interval  $[0, 1]$ . What is the volume of the solid that results when R is revolved about the line  $y = 2$ ?

a.  $\pi \int_0^1 \left[ (2 - x^2)^2 - (2 - x)^2 \right] dx$

b.  $\pi \int_0^1 \left[ (2 - x)^2 - (2 - x^2)^2 \right] dx$

c.  $\pi \int_0^1 \left[ (\sqrt{y})^2 - (y)^2 \right] dy$

d.  $\pi \int_0^1 \left[ (y)^2 - (\sqrt{y})^2 \right] dy$

e.  $\pi \int_0^2 \left[ (2 - y)^2 - (2 - \sqrt{y})^2 \right] dy$

\_\_\_\_\_ 10. A point moves on the x-axis in such a way that its velocity at time  $t$  ( $t > 0$ ) is given by  $v = \frac{\ln t}{t}$ . At what value of  $t$  does  $v$  attain its maximum?

a. 1

b.  $e^{\frac{1}{2}}$

c.  $e$

d.  $e^{\frac{3}{2}}$

e. There is no maximum value of  $v$ .